# Automatic Image Stitching Using SIFT

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## Abstract

This paper concerns the problem of automatic image stitching which mainly applies to the image sequence even those including noise images. And it uses a method based on invariant features to realize fully automatic image stitching, in which it includes two main parts: image matching and image blending. As the noises images have large differences between the other images, when using SIFT features to realize correct and robust matching, it supplies a probabilistic model to verify the panorama image sequence. Addison to have a more satisfied panorama image, it uses a simple and fast blending method which is weighted average method. Finally, the experiment results confirm the feasibility of our methods.

## 1. Introduction

Feature-based method <sup>[1, 2]</sup> is one of methods of Image stitching. And we propose a method based on invariant scale feature <sup>[3, 4, 5]</sup>, which mainly includes two key parts: image matching and image blending. Image matching is used to find the motion relationship between two images or several images, and it directly relates to the success rate and the speed of the total process. While image blending is used to eliminate the various illumination of the adjacent image or color does not consecutive caused by the geometric correction or dynamic scene illumination. In that way two images can stitch into a seamless image.

In our paper, invariant scale features are also called SIFT features. SIFT features are local image features, which keep invariant in rotation, scale or illumination, and also robust in vision changes, affine changes or noises. Consequently, we use the method based on SIFT features, which solve the problem of image matching variant with scale variant in the method based on Harris corner detecting<sup>[6]</sup>. Otherwise, in the actual study, there are some noise images in the

input image sequence. In order to solve this problem we develop a probabilistic model, by matching it to confirm the image and remove interference images. Furthermore, in order to eliminate the stitching visible seams and double edge of the panorama image we use the weighted average method for the image fusion.

# 2. The entire algorithm of the automatic stitching

The entire algorithm mainly includes: extract SIFT features; match features to get potential feature matches; match image sequence; match the image completely and blend the image, which can be described as the figure 1.



## Figre1.The entire process of this paper

## 2.1. Feature extracting

To each image, it builds image pyramid, and subtracts neighbor images to get the difference of Gauss (also called DOG) pyramid. Then, it detects the extreme for DOG pyramid. In order to locate the key points precisely to the sub-pixel accuracy, it fits quadratic function of 3D. At the same time, it eliminates the low contrast key point and the unsteady edge responses to improve the stability of the match. And the following step is orientation assignment, which uses orientation histogram to statistics the gradient orientation with sampling the center neighborhood of the key points. And the last step is to describe to the key points. Moreover, the detail process can be found in referees <sup>[3, 4]</sup>.

## 2.2. Feature matching

We assume the camera rotates about its optical centre, and then the image would undergo a transformation, which can be written as:

$$\tilde{u}_i = H_{ij}\tilde{u}_j \tag{1}$$

Where  $\tilde{u}_j$  is the position before the transformation,  $\tilde{u}_i$  is the position after the transformation, also, the parameter  $H_{ij}$  is deiced by rotational matrix and internal parameter of camera. The general form of  $H_{ij}$  is

$$H_{ij} = \begin{bmatrix} h_{11} & h_{12} & h_{13} \\ h_{21} & h_{22} & h_{23} \\ 0 & 0 & 1 \end{bmatrix}$$
(2)

After extracting features, the next step is to match features by building a K-D tree to find k-nearest neighbors. In this paper, we find four nearest neighbors for each feature. In this way, we could get multiply feature matches.

### 2.3. Image matching

Based on multiply potential feature matches, we describe a modified RANSAC (random sample consensus) to match further. The modified RANSAC can be able to solve the motion relation between the potential feature matches efficiently and robustly, in which the points that satisfy the matrix are called RANSAC inliers, and others are called outliners. Moreover, using the connection of potential features and RANSAC inliers, we can build the probabilities model.

#### 2.3.1. Modified RANSAC method

In our paper, it describes how to use modified middle filter to modify RANSAC. In that way, it can improve the effect of the RANSAC<sup>[7]</sup>, from which we can get the matrix more robustly. As we known, middle filter is formed by two filters: angle filter and length filter. Consequently, we modify them to test the validity of the feature matching.

The rule of the modified angle filters are as following: selecting four feature matches randomly, and computing their entropy. If the entropy is larger than the threshold value, the feature matches can be selected to be the initialize feature matches, otherwise not. Furthermore, the entropy larger, the feature matches more easily picked to be the initial feature matches. The rule of the modified length filters is the same as the rule of angle filters. In shortly, the total algorithm can be shown as below:

- (1) Selecting four feature matches, and using Modified angle filters to test, if satisfying the condition, going to the next step.
- (2) Using modified length filters to test, if satisfying the condition, going to the next step. Otherwise, returning to the former step.
- (3) Computing the transformational matrix.
- (4) Testing whether the all possible feature matches satisfying the condition or not.
- (5) Repeating the upper four steps for N times.
- (6) Finding the feature matches that mostly satisfy the matrixes, and then computing the final matrix using them.

#### 2.3.2. Probabilistic model

From the modified RANSAC, we get lots of features satisfying the affine matrix which are called RANSAC inliers. The method of our probabilistic model is to compare the probabilities of the inliers or outliners was generated by correct or false image match.

As below, we denote the event of the potential feature match *i* is inline or outline as  $f_i$ , and the image match is correct or not as m, which has only two values (0 or 1). Also we label the number of total features as  $n_f$ , and the number of inliers as  $n_i$ . According to the event  $f_i$  and  $f_j$  ( $i \neq j$ ) are independent, we can know that  $f_i$  obey to Bernoulli distribution. So the number of inliers of the overlap can be computed:

 $n_i = n_1 + n_0$ 

where

$$n_{1} = n_{f} \cdot p(f_{i} \mid m = 1) = n_{f} \cdot B(n_{i}, n_{f}, p_{1})$$
  
=  $n_{f} \cdot \frac{n_{f}!}{n_{i}!(n_{f} - n_{i})!} p_{1}^{x} (1 - p_{1})^{n_{f} - n_{i}}$  (4)

(3)

and

$$n_{0} = n_{f} \cdot p(f_{i} | m = 0) = n_{f} \cdot B(n_{i}, n_{f}, p_{0})$$
  
=  $n_{f} \cdot \frac{n_{f}!}{n_{i}!(n_{f} - n_{i})!} p_{0}^{x} (1 - p_{0})^{n_{f} - n_{i}}$  (5)

In the above,  $p_1$  is the probability of the event that the feature is inline under the correct image match; While  $p_0$  is the probability of the event that the feature is inline under false image match.

According to the Bayes rule, we can calculate the condition that the number of inliers and total features should satisfy:

$$n_i > \alpha + \beta \cdot n_f \tag{6}$$

If satisfy the above condition, the image match is correct, otherwise the image match is false. Moreover, the parameter  $\alpha$  and  $\beta$  are decided by the parameter  $p_1$  and  $p_0$ . In this way, we not only verify the matching relationship between images, but also reject the interfere image which is not belong to the panorama image.

## 2.4. Image matching completely

Above all, we have achieved the image match between two images. And in this stage we continue to research image match between multiply images. The key problem is to eliminate the accumulated error between the images, which direct to the success of correct image match. We use bundle adjustment <sup>[8, 9]</sup> to solve the above problem. Firstly, we choose one of the images to be reference surface. Then, each of other images transform to the reference surface, at the end of which all images are on the same surface.

The processes of bundle adjustment are as below: reading each of images into the adjustment, and constantly optimizing the parameters of the matrix in the adjustment. The method of optimizing is: Firstly, finding out the best neighbor image for each image, and directly calculating the distance between the two neighbor images. Then, mining the distance value to adjust the matrix between the neighbor images.

Given that there is one feature match  $(u_i, u_j)$  in the image  $I_i$ , the value of  $u_i$  which is projected to the reference surface and then to its neighbor image become to  $\tilde{u}_i$ . And the residual between them can be shown as:

$$r_{ij} = |u_j - \tilde{u}_i| = |u_j - H_j^{-1} \cdot H_i \cdot u_i|$$
 (7)

where  $H_i$  is the matrix transforming image  $I_i$  to the reference surface, and  $H_j^{-1}$  is the matrix transforming reference surface to the image  $I_j$ .

The object function is the sum of all the residual errors shown as equation (7):

$$e = \sum_{i=1}^{n} \sum_{j \in L(i)} \sum_{k \in F(i,j)} \left| f(r_{ij}^{k}) \right|$$
(8)

where F(i, j) is the set of feature matches between image  $I_i$  and image  $I_i$ . Then, we can update  $H_i$ :

$$H_{i} = H_{ij}' * H_{i}$$
 (9)

where  $H'_{ik}$  is the updating matrix value of image  $I_i$ and its best neighbor image. Furthermore, equitation (8) can be solved by L-M algorithm.

## 2.5. Image blending

The above stages realize image stitching in geometry, which has obvious seam in overlap region. It mainly due to ignoring the difference of illumining <sup>[10]</sup>. Our paper describes average weighed method which is simple and fast for blending, which can be described as figure2.



## Figure2.Blending in the overlap region

In the average weighted blending, the values of features in overlap region are equal to the weighted average values of matching images, which can be shown as following:

$$p = \frac{d_{l}}{d_{l} + d_{r}} p_{l} + \frac{d_{r}}{d_{l} + d_{r}} p_{r}$$
(10)

where  $d_i$  is the distance between the pixel in overlap region to the border of the left matching image, and  $d_r$ is the distance between the pixel in overlap to the border of the right matching image.

# 3. Results

Our paper uses one image sequence sampling in the park, which includes six images in size of  $800 \times 600$ , including a noise image, shown as figure3. And the result of automatic image stitching is shown as figure4. Seeing from the figures4, our method is well effective.





Figure3. One image sequence of the park



Figure4.The output of panorama image

# 4. Conclusions

Our method realizes automatic stitching of disorder image sequence which even includes noise images. Based on extracting invariant scale features, we get potential feature matches by k-nearest neighbor method, and then propose a modified RANSAC algorithm and a probabilistic model to realize image match precisely. Moreover, bundle adjustment is used to reach image match completely. And the average weighed method ensures smooth translation between the overlap regions.

While there are also some insufficiencies in our paper, such as noise would appear in low contrast color image stitching, and ghost would be created when there are moving object in the image sets. And these problems are needed to be solved in our future work.

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